# CS 335: Type Systems

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Content influenced by many excellent references, see References slide for acknowledgements.

### Type Error in Python

def add1(x):
 return x + 1
class A(object):
 pass
a = A()
add1(a)

```
Traceback (most recent call last):
  File "type-error.py", line 8, in <module>
    add1(a)
  File "type-error.py", line 2, in add1
    return x + 1
TypeError: unsupported operand type(s) for
+: 'A' and 'int'
```

### What is a Type?

#### Set of values and operations allowed on those values

- Integer is any whole number in the range  $-2^{31} \le i < 2^{31}$
- enum colors = {red, orange, yellow, green, blue, black, white}

Few types are predefined by the programming language

Other types can be defined by a programmer

• Declaration of a structure in C

### What is a Type?

#### Pascal

 If both operands of the arithmetic operators of addition, subtraction, and multiplication are of type integer, then the result is of type integer

#### C

• "The result of the unary & operator is a pointer to the object referred to by the operand. If the type of operand is X, the type of the result is a pointer to X."

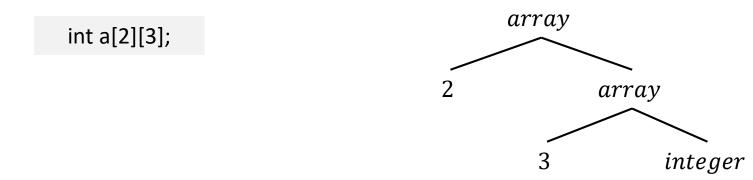
#### Each expression has a type associated with it

# The Meaning of Type

Denotational	<ul> <li>A type is a set of values</li> <li>A value has a given type if it belongs to the set</li> </ul>
Structural	• A type is either from a collection of built-in types or a composite type created by applying a type constructor to built-in types
Abstraction- based	• A type is an interface consisting of a set of operations with well-defined and mutually consistent semantics

#### Type Expression

- Type of a language construct is denoted by a type expression
- A basic type is a type expression
- A type constructor operator applied to a type expression is a type expression



- The set of types and their associated rules are collectively called a type system
  - Rules to associate type expressions to different parts of a program (for e.g., variables, expressions, and functions)
- Type systems include rules for type equivalence, type compatibility, and type inference
- Different type systems may be used by different compilers for the same language
  - Pascal includes the index set of arrays in the type information of a function
  - Compiler implementations allow the index set to be unspecified

# Type Checking

- Ensure that valid operations are invoked on variables and expressions
  - && operator in Java expects two operands of type boolean
- Means both type inferencing and identifying type-related errors
  - A violation of type rules is called type clash
  - Errors like arithmetic overflow is outside the scope of type systems
    - Run-time error, not a type clash
  - Can catch errors, so needs to have a notion for error recovery
- A type checker implements a type system

## Catching Type Errors

- Can a type checker predict that a type error will occur when a particular program is run?
- Impossible to build a type checker that can predict which programs will result in type errors
- Type checkers make a conservative approximation of what will happen during execution
  - Raises error for anything that might cause a type error

### Type Error in Java

```
class A {
int add1(int x) {
return x + 1;
}
```

```
public static void main(String
args[]) {
```

```
A a = new A();
if (false)
add1(a);
```

```
TypeError.java:9: error: incompatible
types: A cannot be converted to int
add1(a);
^
```

Note: Some messages have been simplified; recompile with -Xdiags:verbose to get full output

```
1 error
```

- Strongly typed every expression can be assigned an unambiguous type
  - Statically typed every expression can be typed during compilation
    - Manifest typing requires explicitly identifying the type of a variable during declaration
      - E.g., Pascal and Java
    - Type is deduced from context in implicit typing
      - E.g., Standard ML

<pre>int main() {</pre>	
float $x = 0.0;$	
int y = 0;	
•••	
}	

let val s = "Test"
 val x = 0.0
 val y = 0
...

- Dynamically typed Types are associated with run-time values rather than expressions
  - Type errors cannot be detected until the code is executed
  - E.g., Lisp, Perl, Python, Javascript and Ruby
- Some languages allow both static and dynamic typing
  - For e.g., Java allows downcasting types to subtypes

- Weakly typed Allows a value of one type to be treated as another
  - Errors may go undetected at compile time and even at run time
- Untyped Allows any operation to be performed on any data
  - No type checking is done
  - E.g., assembly, Tcl, BCPL

# Static vs Dynamic Typing

#### Static

- Can find errors at compile time
- Low cost of fixing bugs
- Improved reliability and performance of compiled code
- Effectiveness depends on the strength of the type system

#### Dynamic

- Allows fast compilation
- Type of a variable can depend on runtime information
- Can load new code dynamically
- Allows constructs that static checkers would reject

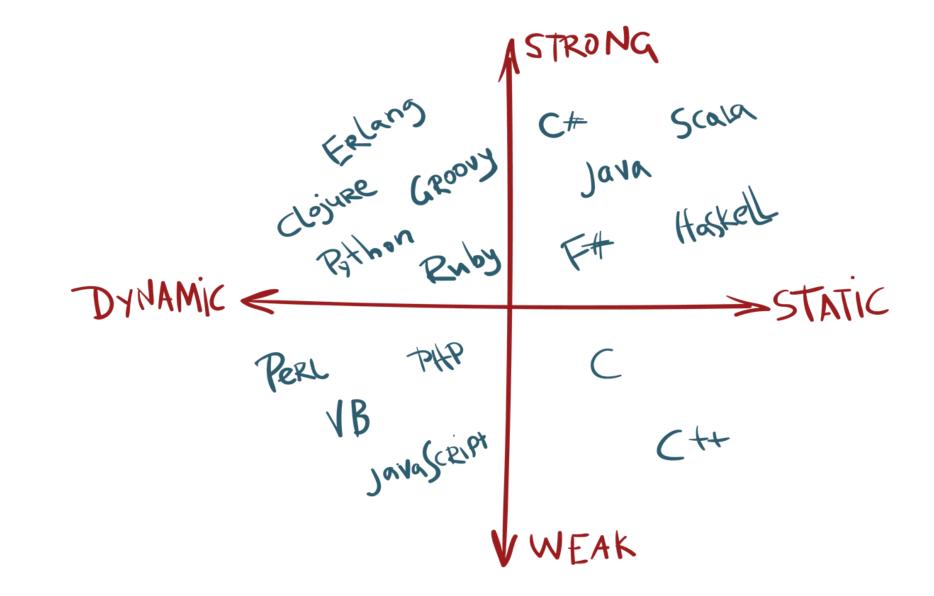
# Type Checking

- All checking can be implemented dynamically
- Sound type system avoids the need for dynamic checking
- A compiler can implement a statically typed language with dynamic checking

# Categorization of Programming Languages

	Statically Typed	Dynamically Typed
Strongly Typed	ML, Haskell, Java, Pascal	Lisp, Scheme
Weakly Typed	C, C++	Perl, PHP

- C is weakly and statically typed
- C++ is statically typed with optional dynamic type casting
- Java is both statically and dynamically typed
- Python is dynamically typed



https://android.jlelse.eu/magic-lies-here-statically-typed-vs-dynamically-typed-languages-d151c7f95e2b

# Gradual Typing

- Allows parts of a program to be either dynamically typed or statically typed
- Programmer controls the typing with annotations
  - Unannotated variables have unknown type
  - Static type checker considers every type to be compatible with unknown
  - Check type at run time

```
def add1(x : int):
    return x + 1
class A(object):
    pass
a = A()
add1(a)
```

https://wphomes.soic.indiana.edu/jsiek/what-is-gradual-typing/

#### Type Hints in Python

def sum(num1: int, num2: int) ->
int:

```
return num1 + num2
```

print(sum(2, 3))

```
print(sum(1, "Hello World!"))
```

• No type checking will happen at run time

# Duck Typing

If it walks like a duck and it quacks like a duck, then it must be a duck

- Duck typing
  - An object's validity is determined by the presence of certain methods and properties, rather than the type of the object itself

```
class Duck:
   def fly(self):
        print("Duck flying")
```

```
class Sparrow:
    def fly(self):
        print("Sparrow flying")
```

```
class Whale:
   def swim(self):
      print("Whale swimming")
```

```
for animal in Duck(), Sparrow(), Whale():
    animal.fly()
```

# TypeScript Example

```
interface Person {
    Name : string;
    Age : number;
}
```

```
function greet(person : Person) {
    console.log("Hello, " + person.N
ame);
```

```
greet({ Name: "svick" });
```

- Compile time error implies that TypeScript uses static structural typing
- Code still compiles to JavaScript
  - Also makes use of dynamic duck typing

https://softwareengineering.stackexchange.com/questions/259941/is-it-possible-to-have-a-dynamically-typed-language-without-duck-typing

# Types of Dynamic Typing

Structural	Nominal
<pre>function greet(person) {</pre>	<pre>function greet(person) {</pre>
if (!(typeof(person.Name) == string && typeof(person.Age) == number)) throw TypeError;	if (!(person instanceof Person)) throw TypeError
<pre>alert("Hello, " + person.Name); }</pre>	<pre>alert("Hello, " + person.Name); }</pre>

https://softwareengineering.stackexchange.com/questions/259941/is-it-possible-to-have-a-dynamically-typed-language-without-duck-typing

# Benefits with Types

## Usefulness of Types

- Type systems help specify precise program behavior
  - Hardware does not distinguish interpretation of a sequence of bits
  - Assigning type to a data variable, called typing, gives meaning to a sequence of bits
- Types limit the set of operations in a semantically valid program
- Types help with documentation
- All the above help reduce bugs

#### Ensure Runtime Safety

- Well-designed type system helps the compiler detect and avoid runtime errors
  - Type inference compiler infers a type for each expression
    - Helps identify misinterpretations of data values
  - Check types of operands of a operator

Result Types for Addition in Fortran 77				
	integer	real	double	complex
integer	integer	real	double	complex
real	real	real	double	complex
double	double	double	double	illegal
complex	complex	complex	illegal	complex

#### Enhanced Expressiveness

- Strong type systems can support other features
  - Operator overloading gives context-dependent meaning to an operator
    - A symbol that can represent different operations in different contexts is overloaded
  - Many operators are overloaded in typed languages
  - In untyped languages, lexically different operators are required
- Strong type systems allow generating efficient code
  - Perform compile-time optimizations, no run-time checks are required
  - Otherwise one needs to maintain type metadata along with value

#### Implementing Addition

#### **Strongly Typed System**

- integer  $\leftarrow$  integer + integer IADD  $R_a, R_b \implies R_{a+b}$
- double  $\leftarrow$  integer + double I2D  $R_a \Rightarrow R_{ad}$ DADD  $R_{ad}, R_b \Rightarrow R_{ad+b}$

#### Weakly Typed System

```
if tag(a) == integer
  if tag(b) == integer
    value(c) = value(a) + value(b)
    tag(c) = integer
  else if tag(b) == real
    temp = converttoreal(a)
    value(c) = temp + value(b)
    tag(c) = real
  else …
else …
```

# Classification of Types

# Components of a Type System

- I. Basic (or built-in) types
- II. Rules for constructing new types from basic types
- III. Method for checking equivalence of two types
- IV. Rules to infer the type of a source language expression

#### Base Types

- Modern languages include types for operating on numbers, characters, and Booleans
  - Similar to operations supported by the hardware
- Individual languages may add additional types
  - Exact definitions and types vary across languages
  - C does not have the string type
- There are two additional basic types
  - void: no type value
  - type error: error during type checking

#### Constructed Types

- Programs often involve ADT concepts like graphs, trees, and stacks
  - Each component of an ADT has its own type
- Constructed types are created by applying a type constructor to one or more base types
  - Also called nonscalar types
  - Examples are arrays, strings, enums, structures, unions
  - Lists in Lisp are constructed type
    - A list is either nil or (cons first rest)
- Constructed types can allow high-level operations
  - Assign one structure variable to another variable

### Constructed Types

Structure	Union
<pre>struct Node {</pre>	union Data {
struct Node* next;	int i;
int value;	float f;
};	char str[16];
	};
Type of Node may be (Node*) x int	<b>Type of</b> Data <b>may be</b> int ∪ float ∪ char[]

#### Type Constructors

- If *T* is a type expression then array(I, T) is a type expression denoting the type of an array with elements of type *T* and index set *I* 
  - *I* is often a range of integers
    - int A[10];
  - A can have type expression array(0...9, integer)
    - C uses equivalent of int\* as the array type
- If  $T_1$  and  $T_2$  are type expressions, then the Cartesian product  $T_1 \times T_2$  is a type expression

#### Type Constructors

- Function maps domain set to a range set
  - Denoted by type expression  $D \rightarrow R$
  - Type of function int \* f(char a, char b) is denoted by char  $\times$  char  $\rightarrow$  int \*
- Type signature is a specification of the types of the formal parameters and return value(s) of a function
  - filter:  $(\alpha \rightarrow \mathbf{boolean}) \times \operatorname{list} \operatorname{of} \alpha \rightarrow \operatorname{list} \operatorname{of} \alpha$
  - filter exhibits parametric polymorphism

#### Type Constructors

 $char \times char \rightarrow pointer(integer)$ 



#### Pointer Types

- If T is a type expression then pointer(T) is a type expression denoting type pointer to an object of type T
- Type safety with pointers assumes addresses correspond to typed objects
- Ability to construct new pointers complicates reasoning about pointer-based computations
  - Some languages allow manipulating pointers
  - Autoincrement and autodecrement constructs new pointers

#### Other Classifications

- Scalar and compound types
  - Discrete, rational, real, and complex types constitute the scalar types
  - Scalar indicates a single value, also called simple types
  - Example of compound types are arrays, maps, sets, and structs
  - String in C is a compound type
- Primitive and reference types
  - Is this directly a value, or is it a reference to something that contains the real value?

# Polymorphism

# Polymorphism

- Use a single interface for entities of multiple types
  - Applicable to both data and functions
  - A function that can operate on arguments of different types is a polymorphic function
  - Built-in operators for indexing arrays, applying functions, and manipulating pointers are usually polymorphic
- Ad hoc, parametric and subtype polymorphism
- Static and dynamic polymorphism

#### Ad hoc Polymorphism

- Explicitly specifies the set of types
- Refers to polymorphic functions that can be applied to arguments of different types
  - Behavior depends on the type of the argument
- E.g., function and operator overloading

String fruits = "Apple" + "Orange";

$$int a = b + c_i$$

#### Parametric Polymorphism

- Code takes type or set of types as parameter, either explicitly or implicitly
- Parametric polymorphism does not specify the exact types
  - Type of the result is a function of the argument types
- Explicit parametric polymorphism is called generics or templates
  - Used mostly in statically-typed languages

```
class List<T> {
  class Node<T> {
    T elem;
    Node<T> next;
  }
  Node<T> head;
  . . .
List<B> map(Func<A, B> f, List<A> x) {
     . . .
```

# Subtype Polymorphism

- Used in object-oriented languages
  - Code is designed to work with values of some specific type *T*
  - Programmer can define extensions of *T* to work with the code

```
abstract class Animal {
    abstract String talk();
class Cat extends Animal {
    String talk() {
        return "Meow!";
class Dog extends Animal {
    String talk() {
        return "Woof!";
void main(String[] args) {
    (new Cat()).talk();
    (new Dog()).talk();
```

#### Static and Dynamic Polymorphism

- Static polymorphism which method to invoke is determined at compile time
  - For e.g., by checking the method signatures (method overloading)
  - Usually used with ad hoc and parametric polymorphism
- Dynamic polymorphism wait until run time to determine the type of the object pointed to by the reference to decide the appropriate method invocation
  - For e.g., by method overriding
  - Usually used with subtype polymorphism

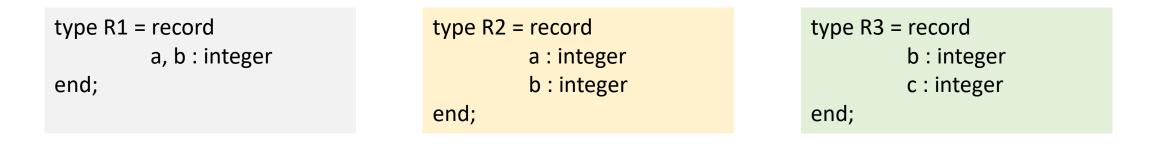
#### Are these definitions the same?

```
struct Tree {
    struct Tree *left;
    struct Tree *right;
    int value;
};
```

struct STree {
 struct STree \*left;
 struct STree \*right;
 int value;
};

#### Are these definitions the same?

- Should the reversal of the order of the fields change type?
  - Some languages say no, most languages say yes



type str = array [1...10] of char;

type str = array [0...9] of char;

- Mechanism to decide the equivalence of two types
- Two approaches
  - Nominal equivalence two type expressions are same if they have the same name (e.g., C++, Java, and Swift)
  - Structural equivalence two type expressions are equivalent if
    - I. Either both are the same basic types,
    - II. or, are formed by applying same type constructor to equivalent types
    - E.g., OCaml and Haskell

Nominal	Structural
class Foo {	class Foo {
<pre>method(input: string): number {     }</pre>	<pre>method(input: string): number {     }</pre>
}	}
class Bar {	class Bar {
<pre>method(input: string): number {    }</pre>	<pre>method(input: string): number {    }</pre>
}	}
let foo: Foo = new Bar(); // ERROR	let foo: Foo = new Bar(); // Okay

https://medium.com/@thejameskyle/type-systems-structural-vs-nominal-typing-explained-56511dd969f4

#### Nominal

- Equivalent if same name
  - Identical names can be intentional
  - Can avoid unintentional clashes
  - Difficult to scale for large projects

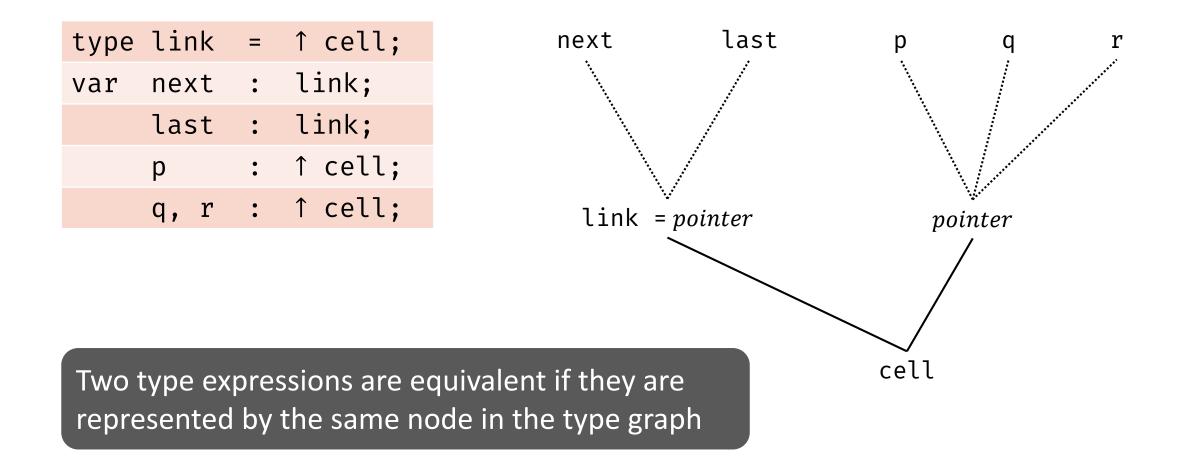
#### Structural

- Equivalent only if same structure
  - Assumes interchangeable objects can be used in place of one other
  - Problematic if values have special meanings

#### Compilers build trees to represent types

• Construct a tree for each type declaration and compare tree structures to test for equivalence

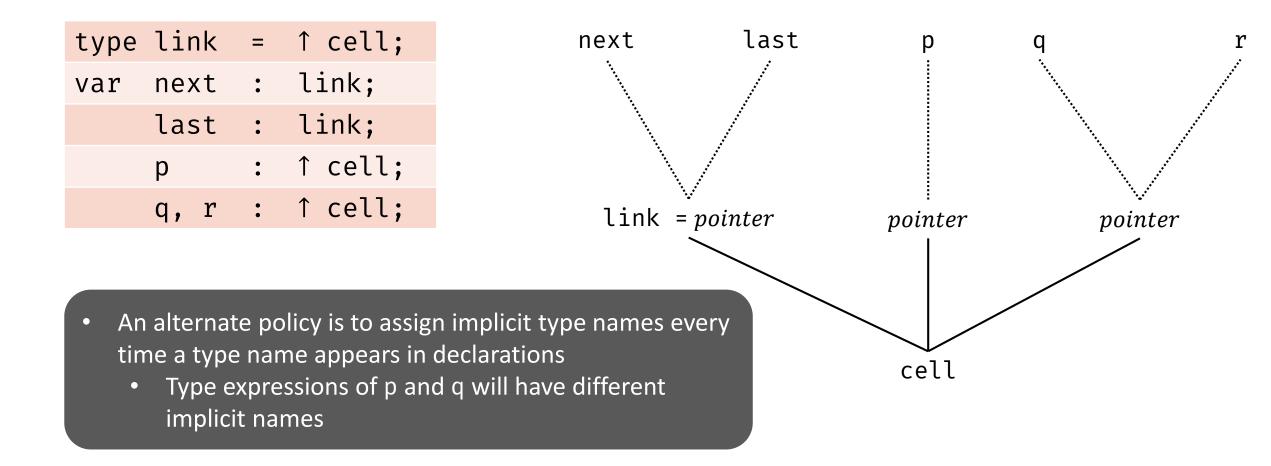
#### Type Graph



#### Type Graph

type	link	=	↑ cell;	next	last	р	q r
var	next	:	link;				
	last	•	link;			* * * * *	
	р	•	↑ cell;			**************************************	/
	q, r	:	↑ cell;	 link =j	pointer	poir	.∝ 1ter
				~		/	
an • Ur	id r are c	of sai	ne type	next and last, and p, q, all the variables are of		cell	

#### Type Graph



#### Testing for Structural Equivalence

```
boolean struc_equiv(type s, type t)
  if s and t are the same basic type then
    return true
  else if s = array(s_1, s_2) and t = array(t_1, t_2) then
    return struc_equiv(s_1, t_1) and struc_equiv(s_2, t_2)
  else if s = s_1 \times s_2 and t = t_1 \times t_2 then
    return struc_equiv(s_1, t_1) and struc_equiv(s_2, t_2)
  else if s = pointer(s_1) and t = pointer(t_1) then
    return struc_equiv(s_1, t_1)
  else if s = s_1 \rightarrow s_2 and t = t_1 \rightarrow t_2 then
    return struc_equiv(s_1, t_1) and struc_equiv(s_2, t_2)
  else
```

return false

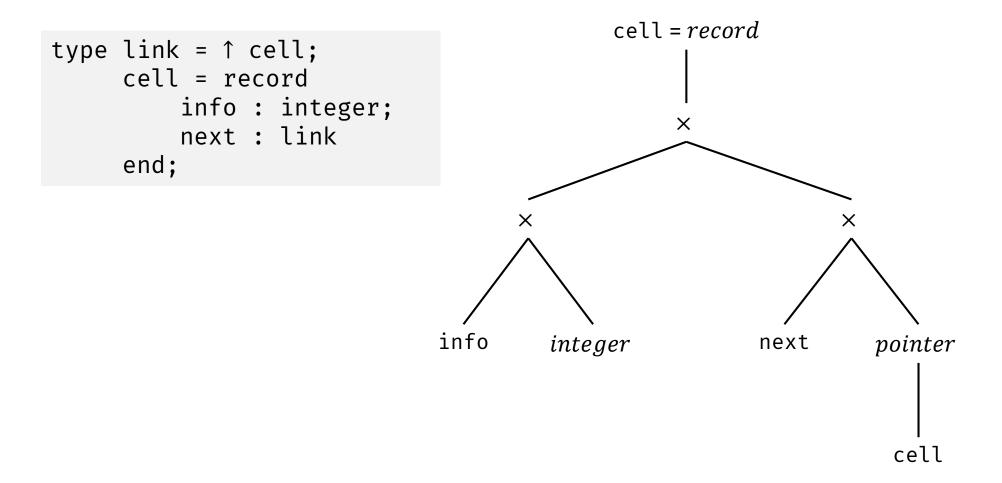
- C uses structural equivalence for scalar types, and uses nominal equivalence for structs
- Language in which aliased types are distinct is said to have strict name equivalence
  - Loose name equivalence implies aliased types are considered equivalent

```
typedef old_type new_type
```

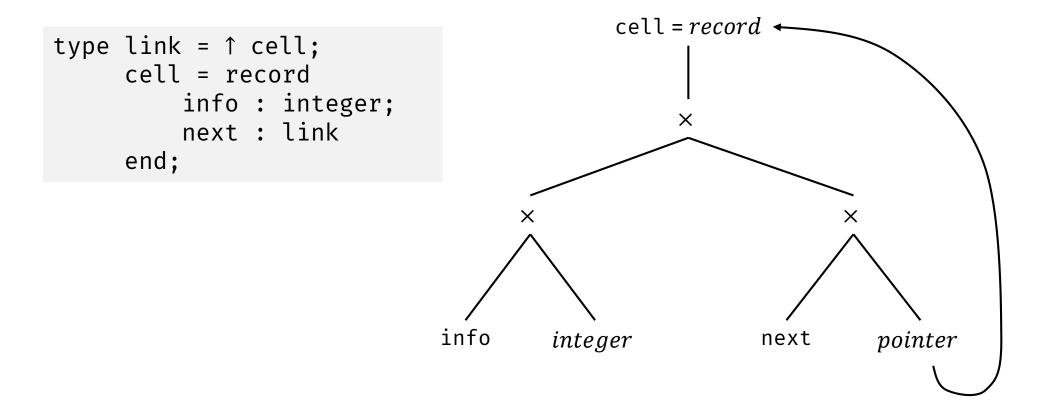
```
int *p, *q, *r;
typedef int * pint;
pint start, end;
```

Variable	Type Expression
р	<pre>pointer(int)</pre>
q	<pre>pointer(int)</pre>
r	<pre>pointer(int)</pre>
start	pint
end	pint

#### Cycles in Representations of Types



#### Cycles in Representations of Types



## Efficient Encoding of Type Expressions

- Bit vectors can be used to encode type expressions
  - More compact than the graph representation
  - *pointer*(*t*) denotes a pointer to type *t*
  - array(t) denotes an array of elements of type t
  - func(t) denotes a function that returns an object of type t

Type Constructor	Encoding
pointer	01
array	10
func	11

Basic Type	Encoding
boolean	0000
char	0001
integer	0010
real	0011

## Efficient Encoding of Type Expressions

Type Constructor	Encoding
pointer	01
array	10
func	11

Basic Type	Encoding
boolean	0000
char	0001
integer	0010
real	0011

Type Expression	Encoding
char	000000 0001
func(char)	000011 0001
<pre>pointer(func(char))</pre>	000111 0001
<pre>array(pointer(func(char)))</pre>	100111 0001

# Efficient Encoding of Type Expressions

Type Constructor	Encoding		Basic Type	Encoding
pointer	01		boolean	0000
array	10		char	0001
func	11		integor	0010
Encoding saves space and also tracks the order of the type constructors in type expressions				
	char		000000 00	001
	func(char)		000011 0001	
po	<pre>pointer(func(char))</pre>		000111 00	001
<pre>array(pointer(func(char)))</pre>		)	100111 00	001

#### Type Compatibility

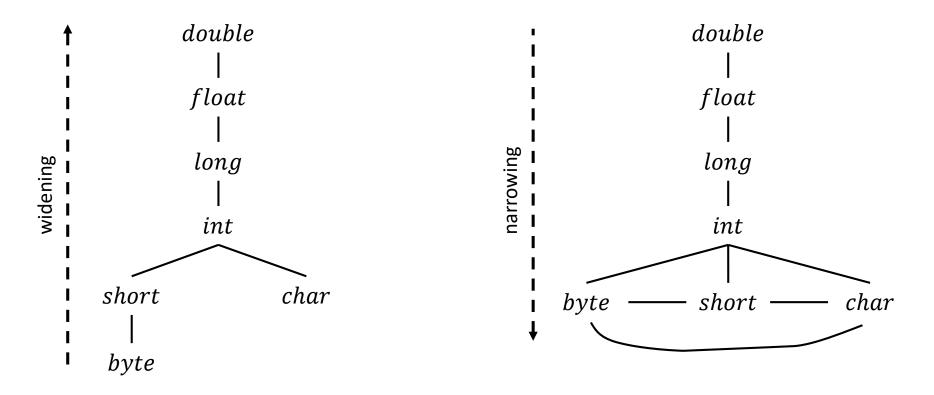
- Most languages do not require equivalence of types in every context
- Type compatibility determines when an object of a certain type can be used in a certain context
- Definitions vary greatly from language to language

#### Type Inference Rules

- Specifies, for each operator, the mapping between the operand types and the result type
  - Type of the LHS of an assignment must be same as the RHS
  - In Java, example, adding two integer types of different precision produces a result of the more precise type
- Some languages require the compiler to perform implicit conversions
  - Internal representations of integers and floats are different in a computer
  - Recognize mixed-type expressions and insert appropriate conversions
  - Implicit type conversion done by the compiler is called **type coercion** 
    - It is limited to the situations where no information is lost

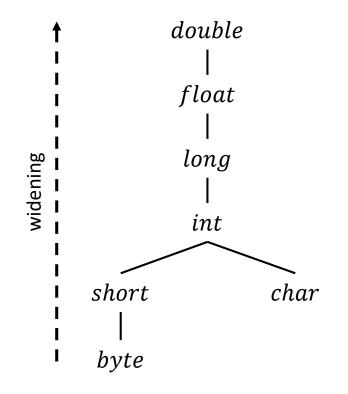
#### Type Conversion

 $\begin{array}{l} E \rightarrow E_1 + E_2 \\ ... \end{array} \begin{array}{l} \{ \text{ if } (E_1. type == integer \text{ and } E_2. type == integer) \ E. type = integer \\ e \text{ lse if } (E_1. type == f \text{ loat and } E_2. type == integer) \ E. type = f \text{ loat} \\ ... \end{array} \right\}$ 



#### Type Conversion

 $E \rightarrow E_1 + E_2 \qquad \{ \text{ if } (E_1. type == integer \text{ and } E_2. type == integer) E. type = integer \\ else \text{ if } (E_1. type == float \text{ and } E_2. type == integer) E. type = float \\ \dots \}$ 

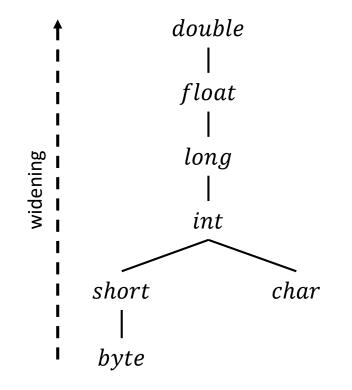


#### Assume two helper functions:

- $\max(t_1, t_2)$  return the maximum (or least common ancestor) of the two types in the hierarchy
- widen(a, t, w) widen a value of type t at address a into a value of type w

#### Type Conversion

{  $E.type = \max(E_1.type, E_2.type)$ ;  $a_1 = widen(E_1.addr, E_1.type, E.type)$ ;  $E \rightarrow E_1 + E_2$   $a_2 = widen(E_2. addr, E_2. type, E. type);$ E.  $addr = new Temp(); gen(E. addr = a_1 "+" a_2);$ 



Assume two helper functions:

- $\max(t_1, t_2)$  return the maximum (or least common ancestor) of the two types in the hierarchy
- widen(a, t, w) widen a value of type t at address a into a • value of type w

#### Type Synthesis for Overloaded Functions

- Suppose *f* is a function
- *f* can have type  $s_i \rightarrow t_i$  for  $1 \le i \le n$ , where  $s_i \ne s_j$  for  $i \ne j$
- x has type  $s_k$  for some  $1 \le k \le n$

• Expression 
$$f(x)$$
 has type  $t_k$ 

# Type Checking

### Type Checking Rules for Coercion from Integer to Real

Production	Semantic Rule
$E \rightarrow num$	E.type = integer
$E \rightarrow $ num . num	E.type = real
$E \rightarrow id$	E.type = lookup(id.entry)
$E \rightarrow E_1 \ op \ E_2$	if $E_1$ . type = integer and $E_2$ . type = integer then E. type = integer else if $E_1$ . type = integer and $E_2$ . type = real then E. type = real else if $E_1$ . type = real and $E_2$ . type = integer then E. type = real else if $E_1$ . type = real and $E_1$ . type = real then E. type = real

Implicit conversion of constants at compile time can reduce run time

# Type Checking

- Some languages allow different levels of checking to apply to different regions of code
- The use strict directive in Javascript and Perl applies stronger checking
- Type checking has also been used for checking for system security

# Type Checking of Expressions

- Idea: build a parse tree, assign a type to each leaf element, assign a type to each internal node with a postorder walk
- Types should be matched for all function calls from within an expression
- Possible ideas
  - I. Require the complete source code
  - II. Make it mandatory to provide type signatures of functions as function prototype
  - III. Defer type checking until linking or run-time

### Specification of a Simple Type Checker

- Simple language where each identifier must be declared before use
- Type checker that can handle statements, functions, arrays, and pointers

 $P \rightarrow D; E$   $D \rightarrow D; D \mid \text{id} : T$   $T \rightarrow \text{char} \mid \text{integer} \mid \text{array} \mid \text{num} \mid \text{of} T \mid \uparrow T$  $E \rightarrow \text{literal} \mid \text{num} \mid \text{id} \mid E \mod E \mid E \mid E \mid E \mid E \uparrow$  key: integer; key mod 1999

# SDT for Manipulating Symbol Table

• SDT to save the type of an identifier

Rules	Semantic Actions
$P \rightarrow D; E$	
$D \rightarrow D; D$	
$D \rightarrow id : T$	{ addtype(id.entry,T.type) }
$T \rightarrow char$	$\{T.type = char\}$
$T \rightarrow integer$	$\{T.type = integer\}$
$T \rightarrow array [num] of T_1$	$\{T.type = array(1num.val, T_1.type)\}$
$T \to \uparrow T_1$	$\{T.type = pointer(T_1.type)\}$

# Type Checking of Expressions

Rules	Semantic Actions
$E \rightarrow $ literal	
$E \rightarrow \mathbf{num}$	
$E \rightarrow id$	
$E \to E_1 \mod E_2$	
$E \to E_1[E_2]$ $E \to E_1 \uparrow$	
$E \rightarrow E_1 \uparrow$	

# Type Checking of Expressions

Rules	Semantic Actions
$E \rightarrow$ literal	$\{ E.type = char \}$
$E \rightarrow \mathbf{num}$	${E.type = integer}$
$E \rightarrow id$	${E.type = lookup(id.entry)}$
$E \to E_1 \mod E_2$	<pre>{ if E<sub>1</sub>.type = integer and E<sub>2</sub>.type = integer then E.type = integer else E.type = type_error }</pre>
$E \to E_1[E_2]$	<pre>{ if E<sub>2</sub>.type = integer and E<sub>1</sub>.type = array(s,t) then E.type = t else E.type = type_error }</pre>
$E \rightarrow E_1 \uparrow$	<pre>{ if E<sub>1</sub>.type = pointer(t) then E.type = t else E.type = type_error }</pre>

# Type Checking of Statements

- Statements do not have values
  - Use the special basic type void

Rules	Semantic Actions
$S \rightarrow \mathbf{id} = E$	
$S \rightarrow \mathbf{if} E \mathbf{then} S_1$	
$S \rightarrow$ while $E$ do $S_1$	
$S \rightarrow S_1; S_2$	

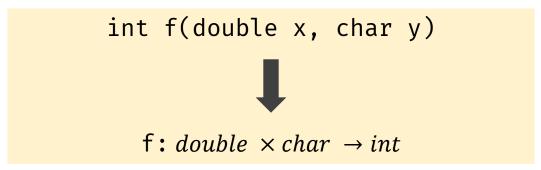
# Type Checking of Statements

- Statements do not have values
  - Use the special basic type void

Rules	Semantic Actions
$S \rightarrow \mathbf{id} = E$	{ <b>if id</b> . <i>type</i> = <i>E</i> . <i>type</i> <b>then</b> <i>S</i> . <i>type</i> = <i>void</i> <b>else</b> <i>S</i> . <i>type</i> = <i>type_error</i> }
$S \rightarrow \mathbf{if} E \mathbf{then} S_1$	{ if $E.type = boolean$ then $S.type = S_1.type$ else $S.type = type\_error$ }
$S \rightarrow$ while $E$ do $S_1$	{ if $E.type = boolean$ then $S.type = S_1.type$ else $S.type = type\_error$ }
$S \rightarrow S_1; S_2$	<pre>{ if S<sub>1</sub>.type = void and S<sub>2</sub>.type = void then S.type = void else S.type = type_error }</pre>

# Type Checking of Functions

Rules	Semantic Actions
$E \to E_1(E_2)$	{ if $E_2$ . $type = s$ and $E_1$ . $type = s \rightarrow t$ then $E$ . $type = t$ else $E$ . $type = type\_error$ }



#### Storage Layout for Local Variables

 $T \rightarrow BC$   $B \rightarrow \text{int}$   $B \rightarrow \text{float}$   $C \rightarrow \epsilon$  $C \rightarrow [\text{ num }] C_1$ 

Determine amount of allocation in a declaration

#### Computing Types and Their Widths

Т	$\rightarrow$	BC
T	$\rightarrow$	BC

 $B \rightarrow int$ 

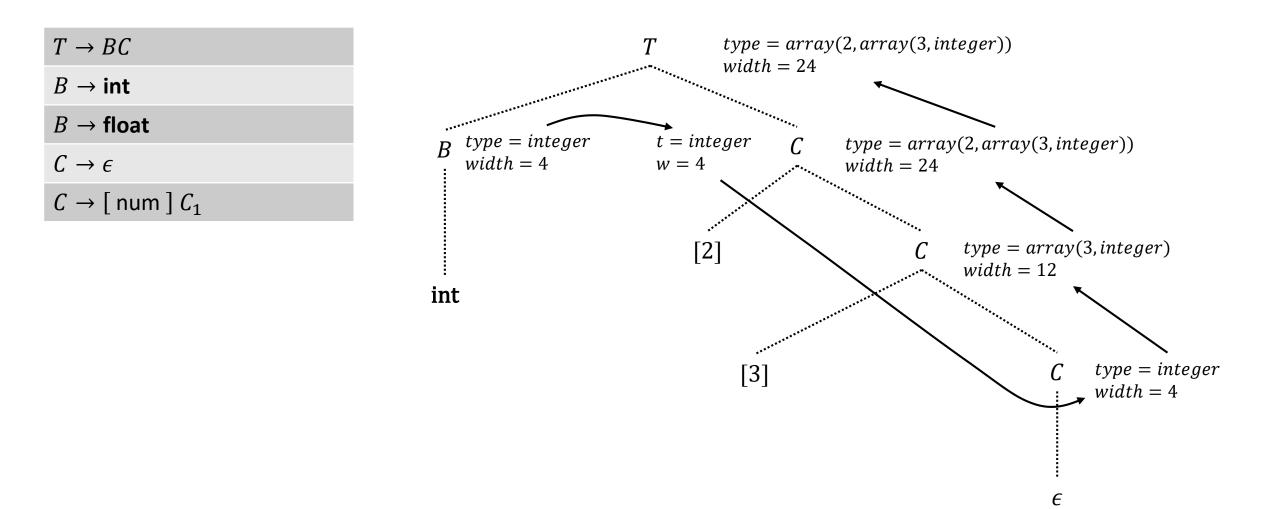
 $B \rightarrow \text{float}$ 

 $C \to \epsilon$ 

 $C \rightarrow [\text{num}] C_1$ 

 $T \rightarrow B \{ t = B.type; w = B.width; \}$   $C \{ T.type = C.type; T.width = C.width; \}$   $B \rightarrow int \{ B.type = integer; B.width = 4; \}$   $B \rightarrow float \{ B.type = float; B.width = 8; \}$   $C \rightarrow \epsilon \{ C.type = t; C.width = w; \}$   $C \rightarrow [num] C_1 \{ C.type = array(num.val, C_1.type);$   $C.width = num.val \times C_1.width; \}$ 

### SDT for Array Type



#### References

- A. Aho et al. Compilers: Principles, Techniques, and Tools, 1<sup>st</sup> edition, Chapter 6.
- K. Cooper and L. Torczon. Engineering a Compiler, 2<sup>nd</sup> edition, Chapter 4.2.
- M. Scott. Programming Language Pragmatics, 4<sup>th</sup> edition, Chapters 7-8.
- <u>https://en.wikipedia.org/wiki/Type\_system</u>